

Word Problems Worksheet

Name: Key

Example 1: The second of two numbers is four more than the first. The sum of the numbers is 56. Find the numbers.

$$\begin{aligned} y &= x + 4 \\ x + y &= 56 \end{aligned}$$

$$\begin{aligned} x + x + 4 &= 56 \\ 2x + 4 &= 56 \\ -4 & \quad -4 \\ \hline 2x &= 52 \\ \frac{2x}{2} &= \frac{52}{2} \\ x &= 26 \end{aligned}$$

$$\begin{aligned} y &= 26 + 4 \\ y &= 30 \end{aligned}$$

$$26 + 30$$

Example 2: Gym A charges a monthly fee of \$20 plus \$2 per time you go to the gym. Gym B only charges \$4 per time you go to the gym. After how many trips to the gym would it cost the same for both? What would that cost be?

$$\begin{aligned} y &= 20 + 2x \\ y &= 4x \end{aligned}$$

$$\begin{aligned} 4x &= 20 + 2x \\ -2x & \quad -2x \\ \hline 2x &= 20 \\ \frac{2x}{2} &= \frac{20}{2} \\ x &= 10 \end{aligned}$$

$$\begin{aligned} y &= 4 \cdot 10 \\ y &= 40 \end{aligned}$$

$$\begin{aligned} &10 \text{ times} \\ &\$40 \end{aligned}$$

1. The sum of two numbers is 90. Their difference is 18. Find the numbers.

$$\begin{aligned} x + y &= 90 \\ x - y &= 18 \\ \hline 2x &= 108 \\ \frac{2x}{2} &= \frac{108}{2} \end{aligned}$$

$$\begin{aligned} x &= 54 \\ 54 + y &= 90 \\ -54 & \quad -54 \\ \hline y &= 36 \end{aligned}$$

$$54 + 36$$

2. The number of girls at Sky High School is 60 greater than the number of boys. If there are 1250 students all together, how many girls and boys are there? $x = \text{boys}$ $y = \text{girls}$

$$\begin{aligned} y &= x + 60 \\ x + y &= 1250 \end{aligned}$$

$$\begin{aligned} x + x + 60 &= 1250 \\ 2x + 60 &= 1250 \\ -60 & \quad -60 \\ \hline 2x &= 1190 \\ \frac{2x}{2} &= \frac{1190}{2} \end{aligned}$$

$$\begin{aligned} x &= 595 \\ y &= 655 \end{aligned}$$

$$\begin{aligned} &655 \text{ girls} \\ &595 \text{ boys} \end{aligned}$$

3. The second of two numbers is 5 more than twice the first. The sum of the numbers is 44. Find the numbers.

$$\begin{aligned} y &= 2x + 5 \\ x + y &= 44 \end{aligned}$$

$$\begin{aligned} x + 2x + 5 &= 44 \\ 3x + 5 &= 44 \\ -5 & \quad -5 \\ \hline 3x &= 39 \\ \frac{3x}{3} &= \frac{39}{3} \\ x &= 13 \end{aligned}$$

$$\begin{aligned} y &= 2(13) + 5 \\ y &= 26 + 5 \\ y &= 31 \end{aligned}$$

$$\begin{aligned} &13 + 31 \end{aligned}$$

4. The number of calories in a piece of pie is 20 less than three times the number of calories in a scoop of ice cream. The pie and ice cream together have 500 calories. How many calories are in each?

$$\begin{aligned} y &= 3x - 20 \\ x + y &= 500 \end{aligned}$$

$x = \text{ice cream}$ $y = \text{pie}$

$$\begin{aligned} x + 3x - 20 &= 500 \\ 4x - 20 &= 500 \\ +20 & \quad +20 \\ \hline 4x &= 520 \\ \frac{4x}{4} &= \frac{520}{4} \end{aligned}$$

$$\begin{aligned} y &= 3(130) - 20 \\ y &= 370 \end{aligned}$$

$$\begin{aligned} &\text{pie} = 370 \\ &\text{ice cream} = 130 \end{aligned}$$

5. Sylvia sold twice as many tickets as Frank. They sold 54 tickets in all. How many did each sell?

$x = \text{Sylvia}$ $y = \text{Frank}$

$$\begin{aligned} x &= 2y \\ x + y &= 54 \end{aligned}$$

$$\begin{aligned} 2y + y &= 54 \\ 3y &= 54 \\ y &= 18 \end{aligned}$$

$$\begin{aligned} x &= 2(18) \\ x &= 36 \end{aligned}$$

$$\begin{aligned} \text{Sylvia} &= 36 \text{ tickets} \\ \text{Frank} &= 18 \text{ tickets} \end{aligned}$$

6. Adult tickets to a play cost \$5 and student tickets cost \$2. In all 720 tickets were sold for a total of \$2640. How many adult and student tickets were sold?

$x = \text{Adult}$ $y = \text{Student}$

$$\begin{aligned} (x + y = 720) \cdot 2 \\ 5x + 2y &= 2640 \end{aligned}$$

$$\begin{aligned} -2x - 2y &= -1440 \\ 3x &= 1200 \\ x &= 400 \end{aligned}$$

$$\begin{aligned} 400 + y &= 720 \\ -400 & \quad -400 \\ y &= 320 \end{aligned}$$

$$\begin{aligned} 400 \text{ adult} \\ 320 \text{ student} \end{aligned}$$

7. One number is 5 more than half of another number. The sum of the numbers is 47. Find the numbers.

$$\begin{aligned} y &= \frac{1}{2}x + 5 \\ x + y &= 47 \end{aligned}$$

$$x + \frac{1}{2}x + 5 = 47$$

$$\begin{aligned} \frac{1}{2}x + 5 &= 47 \\ -5 & \quad -5 \end{aligned}$$

$$\begin{aligned} \frac{1}{2}x &= 42 \\ \frac{1}{2} & \quad \frac{1}{2} \\ x &= 84 \end{aligned}$$

$$\begin{aligned} y &= \frac{1}{2}(84) + 5 \\ y &= 42 + 5 \\ y &= 47 \end{aligned}$$

$$28 + 19$$

8. The length of a rectangle exceeds its width by 3 meters. The perimeter is 58 meters. Find the dimensions.

$x = \text{width}$ $y = \text{length}$

$$\begin{aligned} y &= x + 3 \\ 2x + 2y &= 58 \end{aligned}$$

$$\begin{aligned} 2x + 2(x + 3) &= 58 \\ 2x + 2x + 6 &= 58 \\ -6 & \quad -6 \end{aligned}$$

$$\begin{aligned} 4x &= 52 \\ \frac{4x}{4} & \quad \frac{52}{4} \\ x &= 13 \end{aligned}$$

$$\begin{aligned} y &= 13 + 3 \\ y &= 16 \end{aligned}$$

$$\begin{aligned} \text{length} &= 16 \text{ m} \\ \text{width} &= 13 \text{ m} \end{aligned}$$

9. Two cell phone companies offer texting plans. Company A charges \$5 plus \$0.25 per text. Company B charges \$10 plus \$0.15 per text. After how many texts will it cost the same for Company A and Company B? What will that cost be?

$$\begin{aligned} y &= .25x + 5 \\ y &= .15x + 10 \end{aligned}$$

$$\begin{aligned} .15x + 10 &= .25x + 5 \\ -.15x & \quad -.15x \end{aligned}$$

$$\begin{aligned} 10 &= .10x + 5 \\ -5 & \quad -5 \end{aligned}$$

$$\begin{aligned} 5 &= .10x \\ \frac{5}{.10} & \quad \frac{.10}{.10} \\ x &= 50 \end{aligned}$$

$$y = .25(50) + 5$$

$$\begin{aligned} 50 \text{ texts} \\ \$17.50 \end{aligned}$$

Level 4

10. A grocer wants to mix together some cashews costing \$8 per kilogram with some Brazil nuts costing \$10 per kilogram. The grocer wants to sell 12 kilograms of the mixture for \$8.50 per kilogram. How many kilograms of cashews and Brazil nuts are needed?

$$\begin{aligned} 9 \text{ kg cashews} \\ 3 \text{ kg Brazil nuts} \end{aligned}$$